§4.6: Optimization Problems

1.] What two positive real numbers with a product of 50 have the smallest possible sum?

2.] A vertex of a rectangle is at the origin; the opposite vertex sits in the first quadrant and on the line 2y + x = 4. Find the dimensions that maximize the area of such a rectangle.

3.] Of all boxes with a square base and a volume of 100 m^3 , which one has the smallest minimum surface area?

4.] A farmer has a large rectangular pen that he wishes to subdivide into two adjoining rectangular pens of identical areas. If each pen is to have an area of 1200 square feet, what dimensions will minimize the cost of fencing.

5.] You work for a company that makes jewelry boxes. Your boss tells you that each jewelry box must have a square base and an open top and that you can spend \$3.75 on the materials for each box. The people in production tell you that the material for the sides of the box costs 2 cents per square inch while the reinforced material for the base of the box costs 5 cents per square inch. What is the largest volume jewelry box that you can make and still stay within budget?