By signing below, you attest that you have neither given nor received help of any kind on this exam.

Signature: ____

Printed Name: _

Instructions: Show work to get full credit (the correct answer may NOT be enough). Do all your work on the paper provided. Write clearly! Double check your answers!

You will **not** receive full credit for using methods other than those discussed in class.

For any LP formulation, you do not have to put it in standard form. You also DO NOT have to organize all of the constraints into a nice square form. I will be grading the formulation on the correctness of the decision variables, objective function, and the constraints, not on the presentation or organization of the constraints.

$\begin{array}{c} EXAM \ I \\ {\rm MAT} \ 362 - {\rm Operations} \ {\rm Research} \ {\rm II} \end{array}$

Problem	Available	Your
Number	Points	Points
1	9	
2	6	
3	10	
Total	25	

1. Consider the following LP:

Minimize: $z = 2x_1 + 3x_2$ Subject to: $2x_1 + 3x_2 \le 30$ $x_1 + 2x_2 \ge 10$ $x_1 - x_2 \ge 0$ $x_1, x_2 \ge 0$

(a) Find the dual LP.

(b) For each pair of primal and dual solutions below, determine if they are optimal. In either case, [6] optimal or not, use appropriate justification.

i. Primal: $x_1 = 10, x_2 = 10/3$. Dual: $y_1 = 0, y_2 = 1, y_3 = 1$ [2]

ii. Primal: $x_1 = 20, x_2 = 10$. Dual: $y_1 = 1, y_2 = 4, y_3 = 0$

iii. Primal: $x_1 = 10/3$, $x_2 = 10/3$. Dual: $y_1 = 0$, $y_2 = 5/3$, $y_3 = 1/3$ [2]

[3]

[2]

2. Consider the following LP and its optimal tableau below:

Maximize:	$z = 10x_1 + 4x_2 + 7x_3$									
		Row	Basic	z	x_1	x_2	x_3	s_1	s_2	RHS
Subject to:	$3x_1 + x_2 + 2x_3 \le 7$	0	z	1	0	0	3	2	2	24
		1	x_1	0	1	0	-1	1	-1	2
	$2x_1 + x_2 + 3x_3 \le 5$	2	x_2	0	0	1	5	-2	3	1
	$x_1, x_2, x_3 \ge 0$									

For each sensitivity question below, use information about the dual problem to support your answer.

(a) Assuming the right-hand side of the first constraint represents a resource, what would the optimal objective function value be if only 3 units of this resource were available instead of 7? (Assume the current basis remains optimal.)

(b) The current value of c_3 is 7. For what values of the coefficient c_3 does the current basis remain [2] optimal?

(c) Suppose we add a new variable, x_4 , to the primal problem such that $c_4 = 5$, $a_{14} = 4$ and $a_{24} = -2$. [2] Does the current basis remain optimal?

[2]

3. Consider the unbalanced transportation problem given in the table. If a unit from a source is not shipped [(10)] out (to any of the destinations), a storage cost is incurred at the rate of \$5, \$4, and \$3 per unit for sources 1, 2, and 3, respectively. Additionally, all the supply at source 2 must be shipped out completely to make room for a new product.



(a) Balance the problem by adding a dummy destination and appropriately identify the costs. Then,
[3] establish the initial feasible solution using the Northwest-Corner method.



(b) Solve the problem with a sequence of iterations using the Transportation Simplex method. Please use the grid tableaus provided. Report your optimal solution and the objective function value below.

















